

IMPACT EVALUATION OF OPOWER SMUD PILOT STUDY

UPDATE – September 24, 2009



FINAL REPORT

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October 1, 2009

To Whom It May Concern,

OPOWER is pleased to provide that latest analysis and results for our Home Energy Reporting program at Sacramento Municipal Utility District. The billing data analysis was once again lead by Dan Violette, a founding partner at Summit Blue, a leading measurement & verification firm.

The SMUD program has been running for 16 months and is the longest running program of its kind in the nation. Summit Blue has confirmed the persistence of large energy savings across all 35,000 homes, and has also measured a continuing improvement in program impact over time.

The key findings of the updated report are:

- Year one of program saw a **2.2%** average demand reduction across participating population
Program impact increased to 2.8% in the first four months of year two
- A record-breaking **summer demand reduction of 3.5%** was recorded in 2009
- Impact remain consistent across all major demographic segments

The independent analysis validates OPOWER's own impact assessment of Home Energy Reporting. The same measurement & verification methodology is currently being used to measure and verify the impact of our program at 18 other utilities nationwide. All other deployments are seeing similar levels of energy savings.

For more information about the SMUD program, or the impact of Home Energy Reporting at other utilities, please contact Ogi Kavazovic at ogi@opower.com.

Sincerely,

Alexander Laskey
President
OPOWER, Inc.

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1 EXECUTIVE SUMMARY

Information technologies designed to assist and encourage customers to use less energy are increasing in the industry. OPOWER offers an information program to help customers manage their energy use by providing reports comparing their energy use to the energy use of other similar households. These energy reports provide customers with normative comparisons of their current energy use compared to their neighbors and suggest actions that they can take to reduce their electric use. It is believed that there is a social driver at work in the presentation of energy use in this comparative fashion. If households learn they use more energy than their neighbors, it is assumed they will be motivated to reduce energy use and possibly do more than their neighbors.

OPOWER put this theory to the test with an aggressive experimental design across the Sacramento Municipal Utility District (SMUD). Census blocks were randomly assigned to treatment and control groups. Thirty-five thousand single-family residential customers in the treatment group received regular reports over the period of a year on how their energy use compared to their neighbors' energy use. Fifty thousand single-family customers in the control group did not receive any reports. The pilot began in April 2008. Billing data has been collected for all customers since the start of the program, including one year of billing data from before the test began, to support the impact evaluation of the program.

This report presents Summit Blue's independent third-party impact evaluation of the SMUD experimental design pilot conducted by OPOWER. The updated impact evaluation focuses on answering four basic research questions:

1. Does receiving the reports lead to energy savings?
2. Can the characteristics of large savers be identified?
3. What is the distribution of savings across customers?
4. What is the observed trend for energy savings in the second year of the pilot?

Does receiving the reports lead to energy savings?

Three different statistical methods were used to estimate savings from the program based on analysis of the first year of billing data. Table 1-1 shows that all three methods provided similar results, leading to the conclusion that the reports did indeed encourage customers to reduce their energy use. The estimate of annual savings from each of the three methods ranged from 2.1% to 2.2% showing strong robustness of results. The range around each of these estimates is tight, providing good reliability and precision.

The strength of these estimates rests on the clean design of the experiment and the very large sample sizes that were used. It is often difficult to accurately assess a program savings of 2% from billing analysis because of the wide range of variability in customer bills, but the large scale of this experiment allowed for accurate assessment of savings from this program. Given the consistent estimate of savings found across several methods and the tight range of precision around each estimate, it is clear that the OPOWER reports did encourage a reduction in energy use among customers who received them.

Table 1-1. Comparison of Savings Estimates from Three Statistical Methods

| <i>Method</i> | <i>Average annual kWh savings</i> | <i>95% Confidence interval on avg. annual savings</i> | <i>Average annual percent savings</i> | <i>95% Confidence interval on avg. percent savings</i> |
|--|-----------------------------------|---|---------------------------------------|--|
| <i>Method 1: Difference-in-Difference Statistic</i> | 257 | - | 2.20% | - |
| <i>Method 2: Baseline OLS Linear Model</i> | 253.75 | {216.81, 290.69} | 2.24% | {1.91%, 2.56%} |
| <i>Method 3: Baseline Differenced Linear Fixed Effects Model</i> | 240.88 | {222.81, 258.95} | 2.13% | {1.97%, 2.28%} |

While annual savings were consistently estimated between 2.1% and 2.2%, this is an average of savings that actually varied by season across year one. Table 1-2 uses the difference in difference method to show that savings were the greatest during the summer at 2.6%, followed by a savings of 2.2% during the winter and 1.7% during the other shoulder months. Differences by season are reasonable and expected given that customers use electricity for different purposes during each season. Summer electric use and savings are the highest due to air-conditioning load. Winter use reflects additional lighting and some space heating. The shoulder months have the lowest overall use and savings.

Table 1-2. Savings by Season

| <i>Season</i> | <i>Group</i> | <i>2007 KWH/Day</i> | <i>2008 KWH/Day</i> | <i>Difference KWH/Day</i> | <i>Percent Difference</i> |
|---|---------------|---------------------|---------------------|---------------------------|---------------------------|
| <i>Summer: July, Aug, Sept Billing Months</i> | Participants | 37.53 | 37.10 | -0.43 | |
| | Control Group | 37.83 | 38.37 | +0.54 | |
| | | | | -0.97 | -2.6% |
| <i>Winter: Dec, Jan, Feb, Mar, Apr Billing Months</i> | Participants | 33.19 | 31.56 | -1.63 | |
| | Control Group | 33.34 | 32.45 | -0.89 | |
| | | | | -0.74 | -2.2% |
| <i>Shoulder Months: May, June, Oct, Nov</i> | Participants | 26.58 | 26.73 | +0.15 | |
| | Control Group | 26.91 | 27.52 | +0.61 | |
| | | | | -0.46 | -1.7% |

Participants with low electric use (less than 21.863 kWh/day) received reports quarterly while most participants received reports monthly

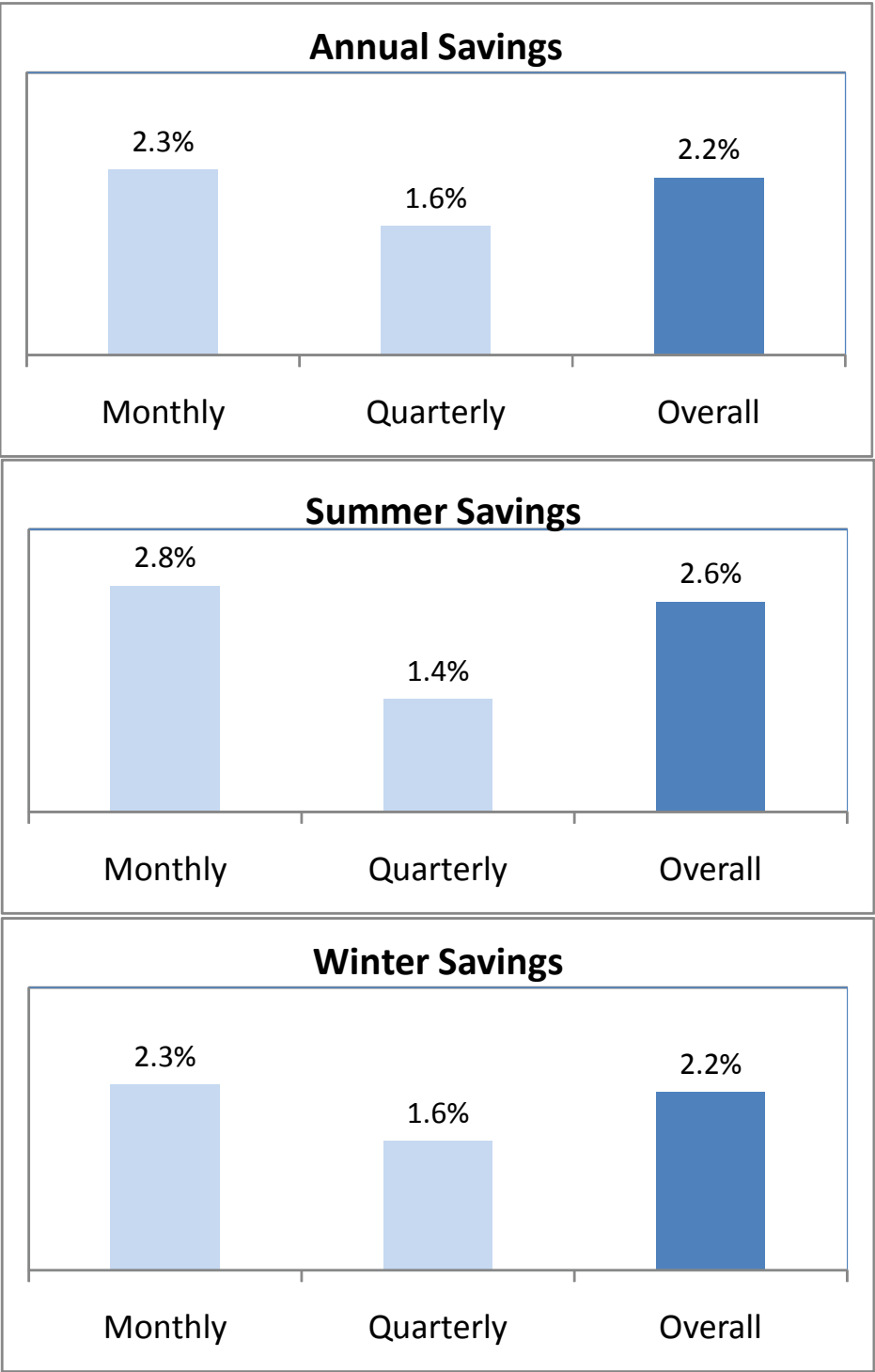
Table 1-3 shows that the high use customers receiving monthly reports achieved greater savings than low use customers receiving quarterly reports. However, both groups achieved savings in each season. Summer was the season showing the greatest savings for high use customers, while low use customers showed relatively consistent savings across all of the seasons.

Table 1-3. Comparison of Savings for Quarterly vs. Monthly Report Recipients

| <i>Method</i> | <i>Summer Impact</i> | <i>Winter Impact</i> | <i>Shoulder Months Impact</i> | <i>Annual Impact</i> |
|--|----------------------|----------------------|-------------------------------|----------------------|
| <i>Monthly Reports (High Use Customers)</i> | -2.8% | -2.3% | -1.9% | -2.3% |
| <i>Quarterly Reports (Low Use Customers)</i> | -1.4% | -1.6% | -1.4% | -1.6% |
| <i>Overall</i> | -2.6% | -2.2% | -1.7% | -2.2% |

These seasonal differences for the different report frequencies are illustrated in **Error! Reference source not found..1** on the next page.

Figure 1-1. Comparison of Savings for Monthly vs. Quarterly Report Recipients



Can the characteristics of large savers be identified?

Both methods 2 and 3 were used to test the contribution of different customer characteristics to savings.

Using method 2, it was found that the only housing characteristics that have a statistically significant effect on energy savings under the program are the presence of a pool and the value of the residence, though as a practical matter the effect of the latter is minor (a \$10,000 increase in home value increases savings by 0.077 Kwh/day). The other housing characteristics examined in the analysis—the presence of a spa, electric space heating, square footage and age of the home—were not statistically significant at the .05 alpha level.

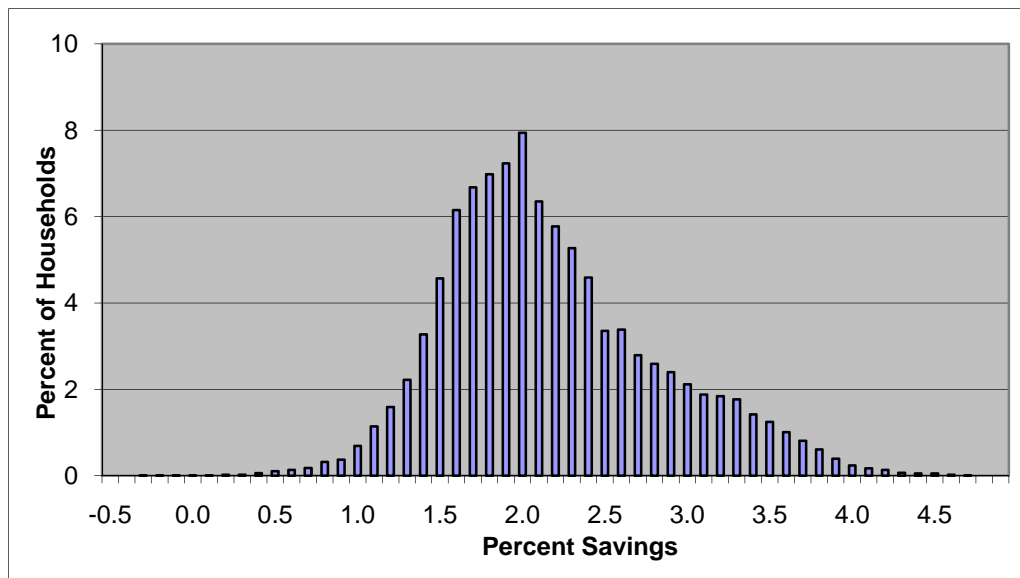
Using method 3, the only housing characteristic affecting energy savings is the presence of a pool.

The upshot of the analysis is that except for the presence/absence of a pool, it is difficult to forecast savings under the program based on housing characteristics. It must be remembered, however, that there is a strong savings response to cooling degree days which indicates that the presence of air conditioning contributes to the overall savings.

What is the distribution of savings across customers?

The method 2 linear regression model was used to predict the distribution of savings within the participant group. Figure 1-2 shows that savings were predicted for nearly all customers. As noted previously, the average savings is about 2.2%. Predicted percent savings for 50% of all households lie in the interval {1.6, 2.2}, predicted savings for 80% of all households lie in the interval {1.4, 2.9}, and predicted savings for 95% of all households lie in the interval {1.1, 3.5}.

Figure 1-2. Frequency distribution of predicted percent annual energy savings (2007 as base year) within the treatment group



This distribution curve shows that savings are predicted for virtually all individuals, rather than being possible for just a small subset of customers with particular characteristics. It is important to emphasize that this frequency distribution describes *expected* savings within the sample, *conditional* on observed housing characteristics such as square footage of the residence, the presence/absence of a pool, the assessed value of the residence, and so forth, based on the point estimates of the OLS regression of method 2. For a given set of housing characteristics, some households in the real world will generate greater savings and some less than indicated in this modeled distribution.

What is the observed trend for energy savings in the second year of the pilot?

Initial analysis based on four months of data from the second year of the pilot, May through August 2009, indicates that the energy savings are going up in the second year. Two of these months, May and June, are Shoulder Months while July and August are part of the Summer season. The difference of differences approach was used to estimate the savings over this entire four month period, and also to give a focused look at what happened over the two summer months.

Table 1-4. Second Year Savings based on Difference of Differences Method

| <i>Period</i> | <i>Group</i> | <i>2007 kWh per Cust</i> | <i>2008 kWh per Cust</i> | <i>2009 kWh per Cust</i> | <i>2007-2008 Difference</i> | <i>Percent Savings</i> | <i>2007-2009 Difference</i> | <i>Percent Savings</i> |
|--|---------------|--------------------------------------|--------------------------------------|--------------------------------------|---------------------------------|----------------------------|---------------------------------|----------------------------|
| May, June, July, and August | Participants | 3,921 | 3,909 | 3,769 | -12 | | -152 | |
| | Control Group | 3,979 | 4,054 | 3,935 | 75 | | -44 | |
| | | | | | -87 | -2.2% | -108 | -2.8% |
| July and August | Participants | 2254 | 2260 | 2165 | 6 | | -89 | |
| | Control Group | 2275 | 2345 | 2266 | 70 | | -9 | |
| | | | | | -64 | -2.8% | -80 | -3.5% |

Table 1.4 shows that looking at both the four month period and the two month summer period, savings increased during the second year of the pilot compared to what was achieved in the first year. During the four month period of May, June, July and August, participants reduced their energy use by 2.2% in 2008 and then achieved even more savings in 2009, dropping their energy use by 2.8% from the base year period. This indicates that there is a cumulative effect to the program and as it continues over time the participants find additional ways to reduce their energy consumption, or, alternatively, additional participants start taking energy saving actions.

The cumulative increase in savings is even more pronounced when focusing only on the high use summer months of July and August. In these two months, participants reduced their energy use by 2.8% in 2008 and then managed to achieve a reduction of 3.5% in 2009. The ability to easily adjust their air-conditioning use, which is typically the largest electric use in homes during these months, is likely to be the cause of these higher summer month savings.

It is of interest to note that savings increased in the second year even while the months of May through August in 2009 were slightly cooler than the same months in 2008.

2 BACKGROUND AND OBJECTIVES

Information technologies designed to assist and encourage customers to use less energy are increasing in the industry. There are a wide variety of information technology options available for accomplishing this purpose. Some focus on hardware solutions that put devices into a customer's home to give them information on current energy use. These devices can be expensive.

OPOWER offers an alternative low cost information program to help customers manage their energy use by providing reports comparing their energy use to the energy use of other similar households. These energy reports provide customers with normative comparisons of their current energy use compared to their neighbors and suggest actions that they can take to reduce their electric use.

It is believed that there is a social driver at work in the presentation of energy use in this comparative fashion. If households learn they use more energy than their neighbors, it is assumed they will be motivated to reduce energy use and possibly do more than their neighbors.

OPOWER put this theory to the test with an aggressive experimental design across the Sacramento Municipal Utility District (SMUD). Census blocks were randomly assigned to treatment and control groups. Thirty-five thousand single-family residential customers in the treatment group received regular reports over the period of a year on how their energy use compared to their neighbors' energy use. Fifty thousand single-family customers in the control group did not receive any reports.

The pilot began in April 2008. Billing data has been collected for all customers since the start of the program, including one year of billing data from before the test began, to support the impact evaluation of the program. Summit Blue provided an initial impact evaluation of the program after one year of test data had been collected. The initial report was issued in May of 2009 and evaluated annual savings and savings by season for the first year. This report is an update of the original and provides results from additional billing data collected for May through August of 2009. Most of this update repeats the results of the first year analysis from the initial report, with updated savings estimates for the first four months of the second year of the pilot presented separately in Section 4.2.

Evaluation Objectives

The impact evaluation which is the focus of this report has both primary and secondary evaluation objectives related to the OPOWER customer reports that were tested in the SMUD pilot.

The primary objective is to answer the basic question:

Does receiving the reports lead to energy savings?

Additional secondary objectives were also identified. These include:

1. What is the distribution of savings across customers?
2. Can the characteristics of large savers be identified?
3. What is the observed trend for energy savings in the second year of the pilot?

The remainder of this report will present the findings to these key evaluation questions.

3 ANALYSIS METHODS

A large set of data generated by a well-constructed experimental design was provided for estimation of impacts of the SMUD Pilot Study. We estimated program impacts using three distinct statistical approaches. Each approach is presented below. Results are presented in section 4.

3.1 Method 1: Difference-in-Difference Statistic

Assuming random assignment of a large number of treatment and control households, a simple difference-in-difference statistic provides a good estimate of the average annual household savings in energy use (measured in kwh) from the treatment.

Denote by \bar{E}_{pg} the average annual rate of kwh use in period p ($p=0$ for the pre-treatment period, $p=1$ for the post-treatment period) by households in group g ($g=0$ for the treatment group, $g=1$ for control group). The difference-in-difference statistic is the difference between the control and treatment groups in the *change* in their annual rate of kwh use across the pre- and post-treatment periods. Formally,

$$\begin{aligned}\Delta E &= (\bar{E}_{11} - \bar{E}_{01}) - (\bar{E}_{10} - \bar{E}_{00}) \\ &= \Delta \bar{E}_1 - \Delta \bar{E}_0\end{aligned}\tag{1}$$

Dividing the difference-in-difference statistic by the average energy use of the control group in the pre-treatment period gives the proportional reduction from treatment,

$$\text{Prop reduction} = \frac{\Delta E}{\bar{E}_{01}}\tag{2}$$

3.2 Method 2: Linear Regression (LR) Models

A second approach is to cast household energy use as a function of a variety of explanatory variables including: a) group membership (treatment vs. control); b) observation period (pre- versus post-treatment); c) relevant weather-related variables such as heating degree days; d) observable housing/household characteristics such as square footage of the residence and the number of household members; and e) an error term reflecting unobservable variables (or alternatively, variables that are not included in the available data set).

The simplest version convenient for exposition is a linear specification in which average daily use (ADU) of kilowatt-hours by household k in month t (where months are assigned consecutively throughout the study period), is a function of three variables: the binary variable $Treatment_k$, taking a value of 0 if household k is assigned to the control group, and 1 if assigned to the treatment group; the binary variable $Post_t$, taking a value of 0 if month t is in the pre-treatment period, and 1 if in the post-treatment period; and the interaction between these variables, $Treatment_k \cdot Post_t$. Formally,

$$ADU_{kt} = \alpha_0 + \alpha_1 Treatment_k + \alpha_2 Post_t + \alpha_3 Treatment_k \cdot Post_t + \varepsilon_{kt}\tag{3}$$

Three observations about this specification deserve comment. First, the treatment response is captured by the coefficient α_3 . This term captures the *difference in the difference* in average daily kwh use between the treatment group and the control group across the pre- and post-treatment periods. In other words,

whereas the coefficient α_2 captures the change in average daily kwh use across the pre- and post-treatment for the *control* group, the sum $\alpha_2 + \alpha_3$ captures this change for the treatment group.

Second, the coefficient α_1 captures the effect of assignment to the treatment group *before* the treatment is actually administered. Given assignment of households to the treatment group via random assignment of census blocks, the *a priori* expected value of α_1 is of course zero, though because the sample of census blocks in the analysis is finite it is not necessarily zero. In other words, including the variable $Treatment_k$ prevents the possibility of bias in the estimate of the treatment effect α_3 that would otherwise exist if households in the treatment group were systematically different than those in the control group.

Third, if the error term ε_{kt} is independent and identically distributed across observations, ordinary least squares (OLS) regression will generate unbiased and efficient estimates. As noted in section 3.3, if the error term includes unobservable housing/household characteristics, then errors are temporally correlated, and ordinary least squares (OLS) regression will generate inefficient parameter estimates. Nonetheless, OLS regression is a useful benchmark, will give good estimates if unobserved household-level effects are negligible, and the method discussed in section 3.3 addresses the case when they are not.

The model can be expanded to include three other types of variables. weather-related variables, housing/household characteristics, and treatment variables reflecting differences in the particular treatment of treatment households. For each of the weather variables and housing characteristics included in estimation, four terms are added: the variable itself; the variable interacted with $Treatment_k$ to capture differential effects due to treatment category; the variable interacted with $Post_t$ to capture differential effects of the variable due to exogenous shocks across the two study periods; and the variable interacted with the interaction $Treatment_k \cdot Post_t$ to capture the effect of the variable on the treatment response.

For each of the treatment variables included in estimation, three terms are added to the model: the variable interacted with $Treatment_k$, the variable interacted with $Post_t$, and the variable interacted with $Treatment_k \cdot Post_t$. This last interaction term captures the effect of the differential treatment on the treatment response.

Formally, defining \mathbf{V}_k as a vector of treatment variables, \mathbf{W}_t as a vector of weather characteristics in month t , and \mathbf{Z}_k as a vector of housing/household characteristics for household k , we have the expanded linear model,

$$\begin{aligned}
ADU_{kt} = & \alpha_0 + \alpha_1 Treatment_k + \alpha_2 Post_t + \alpha_3 Treatment_k \cdot Post_t \\
& + \lambda_1 \mathbf{V}_k \cdot Treatment_k + \lambda_2 \mathbf{V}_k \cdot Post_t + \lambda_3 \mathbf{V}_k \cdot Treatment_k \cdot Post_t \\
& + \beta_0 \mathbf{W}_t + \beta_1 \mathbf{W}_t \cdot Treatment_k + \beta_2 \mathbf{W}_t \cdot Post_t + \beta_3 \mathbf{W}_t \cdot Treatment_k \cdot Post_t \\
& + \delta_0 \mathbf{Z}_k + \delta_1 \mathbf{Z}_k \cdot Treatment_k + \delta_2 \mathbf{Z}_k \cdot Post_t + \delta_3 \mathbf{Z}_k \cdot Treatment_k \cdot Post_t + \varepsilon_{kt}
\end{aligned} \tag{4}$$

where the coefficients λ_t , β_t and δ_t are vector-valued of conformable dimension. In this model, the average daily treatment effect (ADTE) is the sum of all terms multiplying the interaction term $Treatment_k \cdot Post_t$:

$$ADTE_{kt} = \alpha_3 + \lambda_3 \mathbf{V}_k + \beta_3 \mathbf{W}_t + \delta_3 \mathbf{Z}_k . \tag{5}$$

3.3 Method 3: Differenced Linear Fixed Effects (DLFE) Model

The linear regression (LR) models of section 3.2 will generate biased estimates of treatment response if the household-specific error ε_{kt} is correlated with the treatment assignment variable $Treatment_k$. Given the careful experimental design of the study, this seems highly unlikely. However remote the possibility, it can be avoided by estimating a fixed effects model in which a household fixed effects parameter α_{0k} captures all household-specific effects on energy use that do not change over time, including those that are unobservable. With reference to section 3.2 above, and defining φ_k as the household-specific portion of the error, the fixed effects parameter is defined as:

$$\alpha_{0k} = \alpha_0 + \alpha_1 Treatment_k + \lambda_1 \mathbf{V}_k \cdot Treatment_k + \delta_0 \mathbf{Z}_k + \delta_1 \mathbf{Z}_k \cdot Treatment_k + \varphi_k, \quad (6)$$

and the fixed effects model is the corresponding modification of (4):

$$\begin{aligned} ADU_{kt} = & \alpha_{0k} + \alpha_2 Post_t + \alpha_3 Treatment_k \cdot Post_t \\ & + \lambda_2 \mathbf{V}_k \cdot Post_t + \lambda_3 \mathbf{V}_k \cdot Treatment_k \cdot Post_t \\ & + \beta_0 \mathbf{W}_t + \beta_1 \mathbf{W}_t \cdot Treatment_k + \beta_2 \mathbf{W}_t \cdot Post_t + \beta_3 \mathbf{W}_t \cdot Treatment_k \cdot Post_t \\ & + \delta_2 \mathbf{Z}_k \cdot Post_t + \delta_3 \mathbf{Z}_k \cdot Treatment_k \cdot Post_t + \varepsilon_{kt} \end{aligned} \quad (7)$$

In the fixed effect model, estimation of the set of parameters $\{\alpha_0, \alpha_1, \delta_0, \delta_1\}$ in the LR model (4) is replaced by estimation of the fixed effects parameter α_{0k} for *each* household in the sample; in the current study of approximately 85,000 households, this is not a feasible exercise. We instead take advantage of the favorable properties of the fixed effects model—in particular the elimination of the aforementioned potential bias—while avoiding the estimation of the fixed effects parameters, as follows. First, the average of monthly ADU is modeled for each household using (7), by taking the average over all variables (this includes the average of variables that are interactions). Using (7) to average across all such monthly observations for a household gives (where “bars” on variables indicate means):

$$\begin{aligned} \overline{ADU}_k = & \alpha_{0k} + \alpha_2 \overline{Post_t} + \alpha_3 \left(\overline{Treatment_k \cdot Post_t} \right) \\ & + \lambda_2 \left(\overline{\mathbf{V}_k \cdot Post_t} \right) + \lambda_3 \left(\overline{\mathbf{V}_k \cdot Treatment_k \cdot Post_t} \right) \\ & + \beta_0 \overline{\mathbf{W}_t} + \beta_1 \left(\overline{\mathbf{W}_t \cdot Treatment_k} \right) + \beta_2 \left(\overline{\mathbf{W}_t \cdot Post_t} \right) + \beta_3 \left(\overline{\mathbf{W}_t \cdot Treatment_k \cdot Post_t} \right) \\ & + \delta_2 \left(\overline{\mathbf{Z}_k \cdot Post_t} \right) + \delta_3 \left(\overline{\mathbf{Z}_k \cdot Treatment_k \cdot Post_t} \right) + \overline{\varepsilon}_{kt} \end{aligned} \quad (8)$$

Equation (8) is then subtracted from (7) for each household. This generates deviations in monthly household ADU from the household's average monthly ADU . Defining deviations by the symbol " Δ " (so, for instance, the deviation in the dependent variable is $\Delta ADU_{kt} = ADU_{kt} - \overline{ADU}_k$), we have,

$$\begin{aligned}
\Delta ADU_k = & \alpha_{2\Delta} Post_t + \alpha_{3\Delta}(Treatment_k \cdot Post_t) \\
& + \lambda_{2\Delta}(\mathbf{V}_k \cdot Post_t) + \lambda_{3\Delta}(\mathbf{V}_k \cdot Treatment_k \cdot Post_t) \\
& + \beta_{0\Delta} \mathbf{W}_t + \beta_{1\Delta}(\mathbf{W}_t \cdot Treatment_k) + \beta_{2\Delta}(\mathbf{W}_t \cdot Post_t) + \beta_{3\Delta}(\mathbf{W}_t \cdot Treatment_k \cdot Post_t) \\
& + \delta_{2\Delta}(\mathbf{Z}_k \cdot Post_t) + \delta_{3\Delta}(\mathbf{Z}_k \cdot Treatment_k \cdot Post_t) + \Delta \varepsilon_{kt}
\end{aligned} \tag{9}$$

Note that because the fixed effect α_{0k} is the same in every observation period, $\bar{\alpha}_{0k} = \alpha_{0k}$, it is eliminated from (9). Moreover, if ε_{kt} in (7) is an independent and identically distributed normal random variable, then so too is $\Delta \varepsilon_{kt}$, and unbiased parameter estimates are obtained via OLS regression. Finally, the equation generating the estimate of the average daily treatment effect is the same as in the LR model, equation (5).

3.4 Summary of Methods: Relative Strengths and Weaknesses

The difference-in-difference statistic (method 1) has the advantage of simplicity. However, if the assignment of households to the treatment and control groups is not random, or the sample is small, it may deviate substantially from the true treatment effect. Moreover, it provides no information about the effect of household characteristics and treatment variables on program efficacy.

The LR models of method 2 allow examination of the effect of housing/household characteristics on the treatment effect. The main potential disadvantage of these models is that if unobservable housing/household characteristics affecting the treatment response are correlated with assignment to the treatment group—highly unlikely given the careful experimental design of the study—the estimated effect of the average treatment response will be biased. Moreover, correlation of household-level unobservables over time and/or across households will bias the estimates of standard errors and therefore invalidate statistical inference (more on this in the concluding paragraph of this section below).

The DLFE models of method 3 forego the opportunity to estimate the effect of housing/household characteristics on average daily use of kwh in exchange for assuring no bias in estimates of the average treatment response due to correlation between housing/household characteristics and household assignment across the treatment and control groups. All housing/household characteristics that do not change over time—observable and unobservable characteristics alike—are embedded in the fixed effect, which in turn is eliminated from estimation by differencing. It is important to emphasize, though, that estimating the effect of housing characteristics and treatment variables on treatment response *is* possible, because the variables used to measure this effect—interactions involving the variable $Post_t$ —do change over time.

We present the results of all three methods to demonstrate that the estimate of overall savings is robust to the modeling approach. But on theoretical grounds we strongly favor the third method—the DLFE model—because of the role that the household-level fixed effect parameters play in eliminating correlation among errors. This correlation may have severe consequences for statistical inference and may arise for several reasons. The most obvious is that certain unobservable household characteristics likely persist over time. A second is that certain unobservables may be common to households within a neighborhood, causing spatially-correlated errors across households within a neighborhood. Finally, despite the randomization by census block of the assignment of households to the treatment and control

groups, there remains the possibility that households within the control group, or within the treatment group, share certain unobservable characteristics.

In the LR model we account for this last source of correlation by including the treatment variable $Treatment_k$, which effectively removes the correlation from the error term by capturing treatment-specific unobservables in the coefficient α_1 . In the absence of census-block dummy variables in the model, it is possible that α_1 is also capturing spatial correlations across households, because of the block randomization of the experiment. The DLFE model addresses all three sources of correlation by sweeping them into the household-level fixed effects parameter and then eliminating this parameter from estimation by differencing the data. In other words, this approach accounts for household-specific unobservables broadly defined, including neighborhood-level unobservables (a characteristic of the household is its neighborhood) and unobservables possibly arising from the particular grouping of households into treatment vs. control (a characteristic of the household is its assignment to treatment vs. control).

4 FINDINGS

The calculation of the difference-in-difference statistic from (1) is straightforward, but the calculation of energy savings from the LR model (method 2) and the DLFE model (method 3) depends on the particular specification of the models. In the next section we provide the average annual savings generated by the difference-in-difference statistic and the *baseline* LR and DLFE models. In section 4.2, we discuss the baseline LR and DLFE models in more detail, and in section 4.4 we expand the LR model to examine the effect of household characteristics on the treatment response. In section 4.5, we examine the distribution of savings in the population, including the difference in savings between households contacted monthly and those contacted quarterly.

4.1 Estimates of Average Annual Savings

As discussed in the previous section, three different methods were used to estimate average annual savings from the program. Results from each method will now be presented.

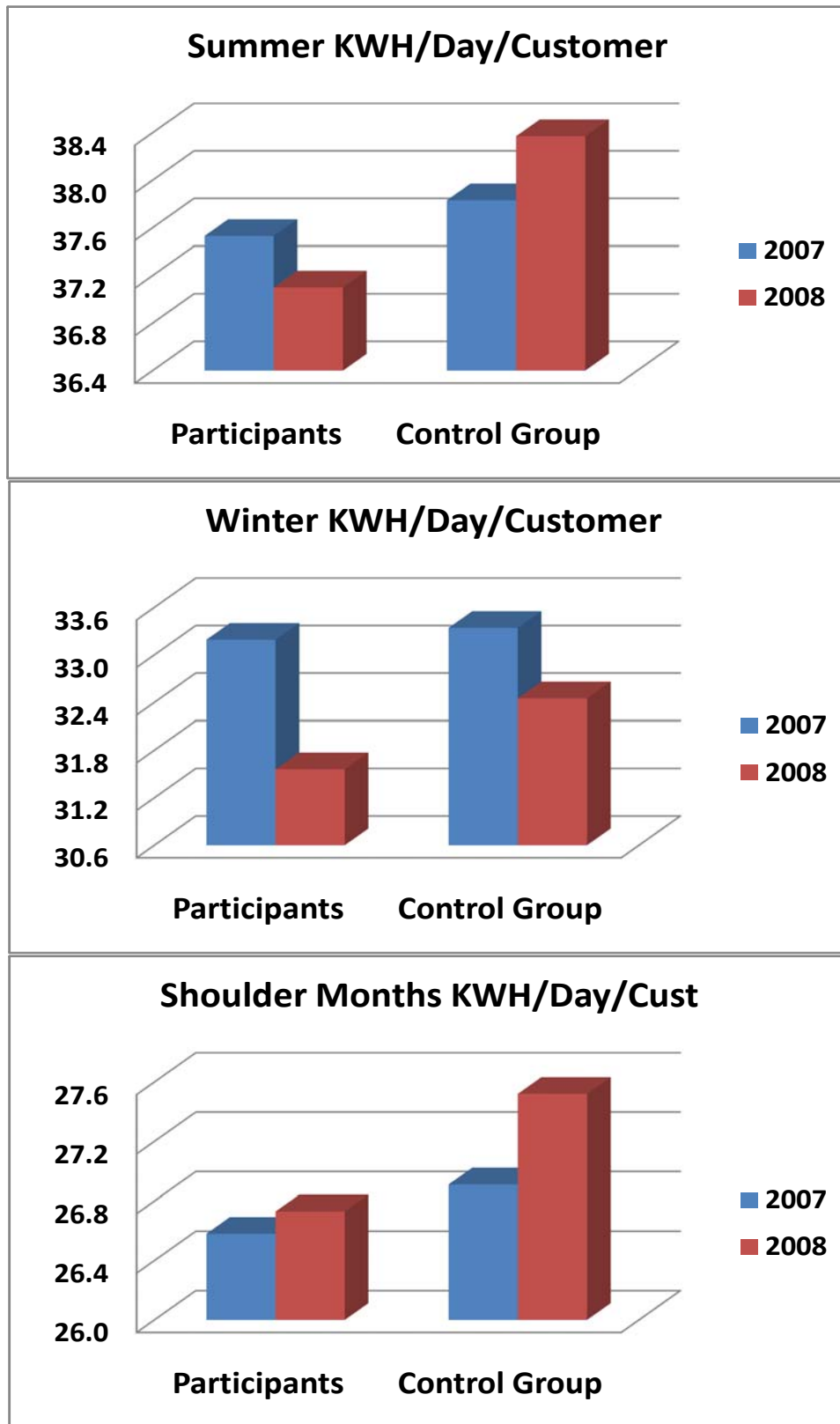
Table 4-1 summarizes the estimation of savings by season using method 1, the difference in differences approach, with the first full year of billing data . It shows that savings were the greatest during the summer at 2.6%, followed by a savings of 2.2% during the winter and 1.7% during the other shoulder months. Differences by season are reasonable and expected given that customers use electricity for different purposes during each season. Summer electric use, and savings, are the highest due to air-conditioning load. Winter use reflects additional lighting and some space heating. The shoulder months have the lowest overall use and savings.

Table 4-1. Savings by Season from Difference in Differences Method

| <i>Season</i> | <i>Group</i> | <i>2007 KWH/Day</i> | <i>2008 KWH/Day</i> | <i>Difference KWH/Day</i> | <i>Percent Difference</i> |
|---|---------------|-------------------------|-------------------------|-------------------------------|-------------------------------|
| <i>Summer: July, Aug, Sept Billing Months</i> | Participants | 37.53 | 37.10 | -0.43 | |
| | Control Group | 37.83 | 38.37 | +0.54 | |
| | | | | -0.97 | -2.6% |
| <i>Winter: Dec, Jan, Feb, Mar, Apr Billing Months</i> | Participants | 33.19 | 31.56 | -1.63 | |
| | Control Group | 33.34 | 32.45 | -0.89 | |
| | | | | -0.74 | -2.2% |
| <i>Shoulder Months: May, June, Oct, Nov</i> | Participants | 26.58 | 26.73 | +0.15 | |
| | Control Group | 26.91 | 27.52 | +0.61 | |
| | | | | -0.46 | -1.7% |

The consistent savings behavior of the participants across all of the seasons can be clearly seen in Figure 4-1. This is most dramatic during the summer when participants reduce their use while control group use increases.

Figure 4-1. Savings by Season from Difference in Differences Method



The observed savings per day by season can be used to estimate the annual savings from the program based on the first full year of data. Table 4-2 shows that the estimated annual savings is 257 kWh per customer which represents a 2.2% reduction in use for participants.

Table 4-2. Annual Savings from Difference in Difference Method

| <i>Method</i> | <i>KWH per Day per Customer Difference</i> | <i>Days per Year</i> | <i>Annual KWH Savings per Customer</i> | <i>Percent Savings</i> |
|------------------------|--|----------------------|--|------------------------|
| <i>Summer</i> | -0.97 | 92 | -89 | |
| <i>Winter</i> | -0.74 | 151 | -112 | |
| <i>Shoulder Months</i> | -0.46 | 122 | -56 | |
| <i>Annual</i> | | | -257 | -2.2% |

Estimated savings from methods 2 and 3 are based on a baseline model specification in which terms concerning heating and cooling degree days are added to the simplest model (3). In particular, the baseline LR model is,

$$ADU_{kt} = \alpha_0 + \alpha_1 Treatment_k + \alpha_2 Post_t + \alpha_3 Treatment_k \cdot Post_t + \beta_{H0} HDDd_t + \beta_{H1} HDDd_t \cdot Treatment_k + \beta_{H2} HDDd_t \cdot Post_t + \beta_{H3} HDDd_t \cdot Treatment_k \cdot Post_t + \beta_{C0} CDDd_t + \beta_{C1} CDDd_t \cdot Treatment_k + \beta_{C2} CDDd_t \cdot Post_t + \beta_{C3} CDDd_t \cdot Treatment_k \cdot Post_t + \varepsilon_{kt} \quad (10)$$

where $HDDd_t$ is heating degree days per day in month t , and $CDDd_t$ is cooling degree days per day in month t . Similarly, the baseline DLFE model is,

$$ADU_{kt} = \alpha_2 Post_t + \alpha_3 Treatment_k \cdot Post_t + \beta_{H0\Delta} HDDd_t + \beta_{H1\Delta} (HDDd_t \cdot Treatment_k) + \beta_{H2\Delta} (HDDd_t \cdot Post_t) + \beta_{H3\Delta} (HDDd_t \cdot Treatment_k \cdot Post_t) + \beta_{C0\Delta} CDDd_t + \beta_{C1\Delta} (CDDd_t \cdot Treatment_k) + \beta_{C2\Delta} (CDDd_t \cdot Post_t) + \beta_{C3\Delta} (CDDd_t \cdot Treatment_k \cdot Post_t) + \varepsilon_{kt} \quad (11)$$

From (5), for both models the effect of treatment on average daily Kwh use—the average daily treatment effect (ADTE)— is,

$$ADTE_t = \alpha_3 + \beta_{H3} HDDd_t + \beta_{C3} CDDd_t \quad (12)$$

Expanding (12) by using 2007 values of $HDDd_t$ and $CDDd_t$ generates the equation used in the calculation of annual savings due to the treatment effect ($AnnTE$) reported in Table 4-3:

$$AnnTE = \alpha_3 \cdot 365 + \beta_{H3} \cdot 2622 + \beta_{C3} \cdot 853 \quad (13)$$

Table 4-3 compares the estimated annual savings from each of the three methods. Two results deserve comment. First, all three methods give approximately the same result of an annual savings of about 2.1-2.2%. We found this result to hold across a wide variety of model specifications. Second, these estimates are very reliable, having a range of 1.9 to 2.6% at the 95% confidence level. The confidence intervals for methods 2 and 3 were calculated using the delta method (Greene 2002). They reflect the degree of precision in model parameter estimates, and are based on energy use in the sample in 2007 (the pre-

treatment period), and thus on heating and cooling degree days in 2007. Along with the mean savings, these intervals would expand or contract somewhat depending on annual weather.

Table 4-3. Summary of Average Annual KWH Savings

| <i>Method</i> | <i>Average annual kWh savings</i> | <i>95% Confidence interval on avg. annual savings</i> | <i>Average annual percent savings</i> | <i>95% Confidence interval on avg. percent savings</i> |
|--|-----------------------------------|---|---------------------------------------|--|
| <i>Method 1: Difference-in-Difference Statistic:</i> | 257 | - | 2.20% | - |
| <i>Method 2: Baseline OLS Linear Model</i> | 253.75 | {216.81, 290.69} | 2.24% | {1.91%, 2.56%} |
| <i>Method 3: Baseline Differenced Linear Fixed Effects Model</i> | 240.88 | {222.81, 258.95} | 2.13% | {1.97%, 2.28%} |

4.2 New Results with Additional Data

This section presents updated savings results for the first four months of the second year of the pilot, May through August 2009. Two of these months, May and June, are Shoulder Months while July and August are part of the Summer season. This update uses the difference of differences approach to estimate the savings seen in the additional data. First we will look at total savings over the new four months, and then we will give a focused look at what happened over the two summer months.

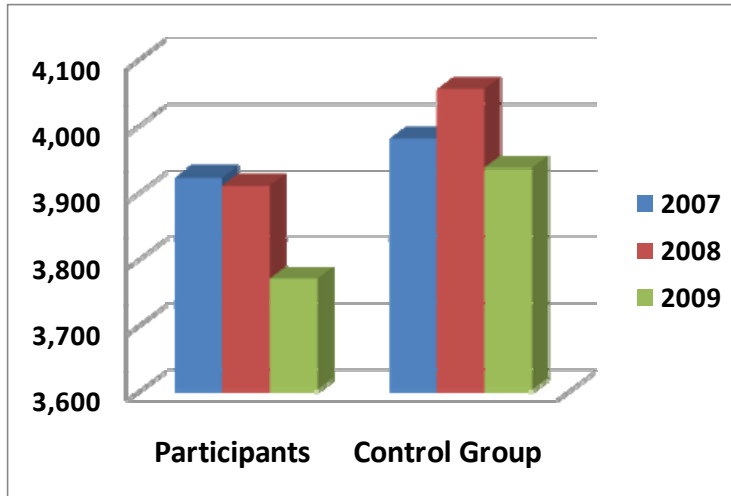
Table 4-4. Second Year Savings based on Difference of Differences Method

| <i>Period</i> | <i>Group</i> | <i>2007 kWh per Cust</i> | <i>2008 kWh per Cust</i> | <i>2009 kWh per Cust</i> | <i>2007-2008 Difference</i> | <i>Percent Savings</i> | <i>2007-2009 Difference</i> | <i>Percent Savings</i> |
|------------------------------------|---------------|--------------------------|--------------------------|--------------------------|-----------------------------|------------------------|-----------------------------|------------------------|
| May, June, July, and August | Participants | 3,921 | 3,909 | 3,769 | -12 | | -152 | |
| | Control Group | 3,979 | 4,054 | 3,935 | 75 | | -44 | |
| | | | | | -87 | -2.2% | -108 | -2.8% |
| July and August | Participants | 2254 | 2260 | 2165 | 6 | | -89 | |
| | Control Group | 2275 | 2345 | 2266 | 70 | | -9 | |
| | | | | | -64 | -2.8% | -80 | -3.5% |

Table 4.4 shows that looking at both the four month period and the two month summer period, savings increased during the second year of the pilot compared to what was achieved in the first year. During the four month period of May, June, July and August, participants reduced their energy use by 2.2% in 2008

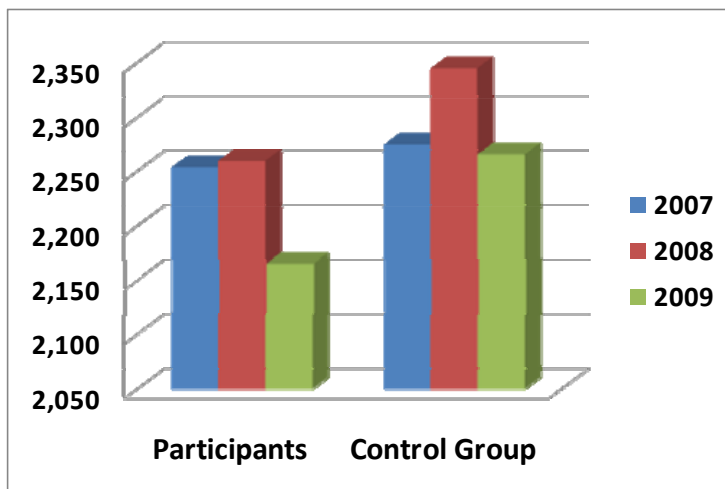
and then achieved even more savings in 2009, dropping their energy use by 2.8% compared to the base year period. This indicates that there is a cumulative effect to the program and as it continues over time the participants find additional ways to reduce their energy consumption, or, alternatively, additional participants start taking energy saving actions. Figure 4.2 illustrates how average kWh per customer changed for the participants and the control group during these four months over the study timeframe.

Figure 4-2. Average kWh per Customer for May, June, July and August



The cumulative increase in savings is even more pronounced when focusing only on the high use summer months of July and August. In these two months, participants reduced their energy use by 2.8% in 2008 and then managed to achieve a reduction of 3.5% in 2009. The ability to easily adjust their air-conditioning use, which is typically the largest electric use in homes during these months, is likely to be the cause of these higher summer month savings. Figure 4.3 shows average kWh use for these two months.

Figure 4-3. Average kWh per Customer for July and August



It is of interest to note that savings increased in the second year even while the months of May through August in 2009 were slightly cooler than the same months in 2008.

4.3 Differential Effect of Heating/Cooling Degree Days on Treatment and Control Households

Parameter estimates derived from the baseline LR model (10) are presented in Table 4-5, and estimates of the same parameters derived from the baseline DLFE model (11) are presented in Table 4.6.

Parameter estimates are interpreted as the marginal effect of a change in the variable on energy use. So, for instance, the LR model indicates that a 1-unit increase in heating degrees days per day increases average daily consumption of energy by .739 Kwh, while the DLFE model indicates such a change would increase average daily consumption by .730 Kwh.

The models are in good agreement with regard to the average daily treatment effect (see equation (12)). The LR model indicates that on a day free of heating and cooling degree days, the treatment reduces consumption of energy by 0.448 Kwh; each heating degree day adds 0.0182 to the savings, and each cooling degree day adds 0.0498 to the savings. These figures for the DLFE model are 0.326, 0.0245, and 0.0675, respectively. In the DLFE model, all treatment terms are significant at the .01 level. Estimates of the treatment effects in the LR model are less precise; the treatment terms $Treatment_k \cdot Post_t$ and $CDDd_t \cdot Treatment_k \cdot Post_t$ are significant at the .05 level, and the treatment term $HDDd_t \cdot Treatment_k \cdot Post_t$ is significant at the .08 level.

Table 4-5. Parameter estimates using the baseline Linear Regression (LR) Model (Dependent variable: Average daily Kwh; treatment terms shaded)

| <i>Variable</i> | <i>Parameter estimate</i> | <i>Standard error</i> | <i>t-statistic</i> |
|--|---------------------------|-----------------------|--------------------|
| <i>Intercept</i> | 20.03454 | 0.05397 | 371.24 |
| <i>Treatment_k</i> | -0.34995 | 0.08422 | -4.16 |
| <i>Post_t</i> | 1.01504 | 0.08935 | 11.36 |
| <i>Treatment_k · Post_t</i> | -0.44838 | 0.13928 | -3.22 |
| <i>HDDd_t</i> | 0.73943 | 0.00393 | 188.39 |
| <i>HDDd_t · Post_t</i> | -0.06662 | 0.00664 | -10.04 |
| <i>HDDd_t · Treatment_k</i> | 0.00277 | 0.00612 | 0.45 |
| <i>HDDd_t · Treatment_k · Post_t</i> | -0.01815 | 0.01036 | -1.75 |
| <i>CDDd_t</i> | 2.49685 | 0.01061 | 235.42 |
| <i>CDDd_t · Post_t</i> | -0.30645 | 0.01588 | -19.3 |
| <i>CDDd_t · Treatment_k</i> | -0.03342 | 0.01652 | -2.02 |
| <i>CDDd_t · Treatment_k · Post_t</i> | -0.04983 | 0.0247 | -2.02 |

Table 4-6. Parameter estimates using the baseline Differenced Linear Fixed Effects (DLFE) model (Dependent variable: Average daily Kwh)

| <i>Variable</i> | <i>Parameter estimate</i> | <i>Standard error</i> | <i>t-statistic</i> |
|---|---------------------------|-----------------------|--------------------|
| $Post_t$ | -0.13361 | 0.04369 | -3.06 |
| $Treatment_k \cdot Post_t$ | -0.32591 | 0.0681 | -4.79 |
| $HDDd_t$ | 0.73034 | 0.00192 | 380.76 |
| $HDDd_t \cdot Post_t$ | -0.01074 | 0.00324 | -3.31 |
| $HDDd_t \cdot Treatment_k$ | 0.0041 | 0.00299 | 1.37 |
| $HDDd_t \cdot Treatment_k \cdot Post_t$ | -0.02453 | 0.00506 | -4.85 |
| $CDDd_t$ | 2.44219 | 0.00518 | 471.24 |
| $CDDd_t \cdot Post_t$ | -0.16486 | 0.00776 | -21.24 |
| $CDDd_t \cdot Treatment_k$ | -0.02305 | 0.00807 | -2.86 |
| $CDDd_t \cdot Treatment_k \cdot Post_t$ | -0.06754 | 0.01208 | -5.59 |

4.4 Extending the Analysis: The Effect of Housing Characteristics and Treatment Variables on Energy Savings

To the baseline models we added the following housing characteristics to examine the effect of these characteristics on energy savings under treatment:

- A binary variable indicating the presence of a pool ($Pool_k$ takes a value of 1 if household k has a pool, and 0 otherwise);
- A binary variable indicating the presence of a spa (Spa_k takes a value of 1 if household k has a spa, and 0 otherwise);
- An interaction term multiplying a binary variable indicating the presence of electric heat ($Eheat_k$ takes a value of 1 if household k has electric heat, and 0 otherwise) by the heating degree days per day, $HDDd_t$;
- Square footage of the residence ($Sqft_k$), measured in units of 100 square feet;
- Age of the residence (Age_k) measured in years; and
- The assessed value of the property ($Value_k$) measured in \$10,000 of assessed value.

A number of household characteristics for which data was available (income, age of head of household, number of household members, length of residence) were excluded from the analysis because preliminary

analyses indicated these variables did not affect the treatment response and because using these variables would significantly reduce the sample size.

We also included in estimation two treatment variables: $Template_k$ is a binary variable taking a value of 1 if a household is assigned a “graphical” presentation of information and 0 for the “narrative” presentation of information. $Envelope_k$ is a binary variable taking a value of 1 if a household receives its material in a large (6x9) envelope and a 0 if it receives its material in a regular business envelope.

Results are presented in Table 4-7 (LR model) and Table 4-8 (DLFE model). As in the baseline models, coefficients reflect the marginal effect of the characteristic on average daily consumption of Kwh. So, for instance, results from the LR model indicate that a 100-ft² increase in the size of a residence increases average daily consumption of Kwh by 0.772; a pool increases average daily Kwh use by 10.90 Kwh.

In the LR model, the only housing characteristics that have a statistically significant effect on energy savings under the program are the presence of a pool and the value of the residence, though as a practical matter the effect of the latter is minor (a \$10,000 increase in home value increases savings by 0.077 Kwh/day. The other housing characteristics examined in the analysis— Spa_k , $Eheat_k$, $Sqft_k$, and Age_k —were not statistically significant at the .05 alpha level.

In the DLFE model (Table 4-8), the only housing characteristic affecting energy savings is the presence of a pool. The upshot of the analysis is that except for the presence/absence of a pool, it is difficult to forecast savings under the treatment program based on housing characteristics.

Finally, neither model predicts that energy savings under the program is affected by the treatment variables $Envelope_k$ and $Template_k$.

Table 4-7. Parameter estimates using the extended Linear Regression (LR) Model (Dependent variable: Average daily Kwh; terms affecting treatment response are shaded)

| <i>Variable</i> | <i>Parameter estimate</i> | <i>Standard error</i> | <i>t-statistic</i> |
|--|---------------------------|-----------------------|--------------------|
| <i>Intercept</i> | 2.58923 | 0.08741 | 29.62 |
| <i>Treatment_k</i> | 1.16059 | 0.13963 | 8.31 |
| <i>Post_t</i> | 1.4126 | 0.14112 | 10.01 |
| <i>Treatment_k·Post_t</i> | -0.1095 | 0.22251 | -0.49 |
| <i>HDDd_t</i> | 0.42534 | 0.00334 | 127.39 |
| <i>HDDd_t·Post_t</i> | -0.03041 | 0.00564 | -5.39 |
| <i>HDDd_t·Treatment_k</i> | -0.00836 | 0.00522 | -1.6 |
| <i>HDDd_t·Treatment_k·Post_t</i> | -0.01879 | 0.00882 | -2.13 |
| <i>CDDd_t</i> | 2.47496 | 0.00872 | 283.91 |
| <i>CDDd_t·Post_t</i> | -0.25433 | 0.01305 | -19.49 |
| <i>CDDd_t·Treatment_k</i> | -0.02555 | 0.01358 | -1.88 |
| <i>CDDd_t·Treatment_k·Post_t</i> | -0.06357 | 0.02031 | -3.13 |
| <i>Pool_k</i> | 10.90364 | 0.04539 | 240.25 |

| | | | |
|---|----------|---------|--------|
| $Pool_k \cdot Post_t$ | 0.01959 | 0.07028 | 0.28 |
| $Pool_k \cdot Treatment_k$ | -0.12378 | 0.07189 | -1.72 |
| $Pool_k \cdot Treatment_k \cdot Post_t$ | -0.69719 | 0.1114 | -6.26 |
| Spa_k | 0.7963 | 0.09075 | 8.78 |
| $Spa_k \cdot Post_t$ | 0.03275 | 0.14022 | 0.23 |
| $Spa_k \cdot Treatment_k$ | 0.40093 | 0.14198 | 2.82 |
| $Spa_k \cdot Treatment_k \cdot Post_t$ | -0.31411 | 0.21966 | -1.43 |
| $Eheat_k$ | 1.26684 | 0.00345 | 367.46 |
| $Eheat_k \cdot Post_t$ | -0.06718 | 0.00586 | -11.46 |
| $Eheat_k \cdot Treatment_k$ | -0.02382 | 0.00534 | -4.46 |
| $Eheat_k \cdot Treatment_k \cdot Post_t$ | -0.01397 | 0.00909 | -1.54 |
| $Sqft_k$ | 0.7717 | 0.00371 | 208.24 |
| $Sqft_k \cdot Post_t$ | -0.02808 | 0.00575 | -4.88 |
| $Sqft_k \cdot Treatment_k$ | -0.03334 | 0.0059 | -5.65 |
| $Sqft_k \cdot Treatment_k \cdot Post_t$ | -0.01467 | 0.00916 | -1.6 |
| Age_k | -0.00408 | 0.00102 | -4.02 |
| $Age_k \cdot Post_t$ | -0.0167 | 0.00158 | -10.57 |
| $Age_k \cdot Treatment_k$ | -0.01144 | 0.00158 | -7.24 |
| $Age_k \cdot Treatment_k \cdot Post_t$ | 0.00116 | 0.00246 | 0.47 |
| $Value_k$ (per \$10,000) | 0.07725 | 0.00143 | 54.04 |
| $Value_k \cdot Post_t$ | 0.0142 | 0.00222 | 6.4 |
| $Value_k \cdot Treatment_k$ | -0.00981 | 0.00228 | -4.31 |
| $Value_k \cdot Treatment_k \cdot Post_t$ | 0.00636 | 0.00354 | 1.8 |
| $Envelope_k \cdot Treatment_k$ | 0.02942 | 0.04088 | 0.72 |
| $Envelope_k \cdot Post_t$ | 0.06717 | 0.04043 | 1.66 |
| $Envelope_k \cdot Treatment_k \cdot Post_t$ | -0.1137 | 0.07544 | -1.51 |
| $Template_k \cdot Treatment_k$ | -0.18351 | 0.04088 | -4.49 |
| $Template_k \cdot Post_t$ | -0.06236 | 0.04043 | -1.54 |
| $Template_k \cdot Treatment_k \cdot Post_t$ | 0.07479 | 0.07543 | 0.99 |

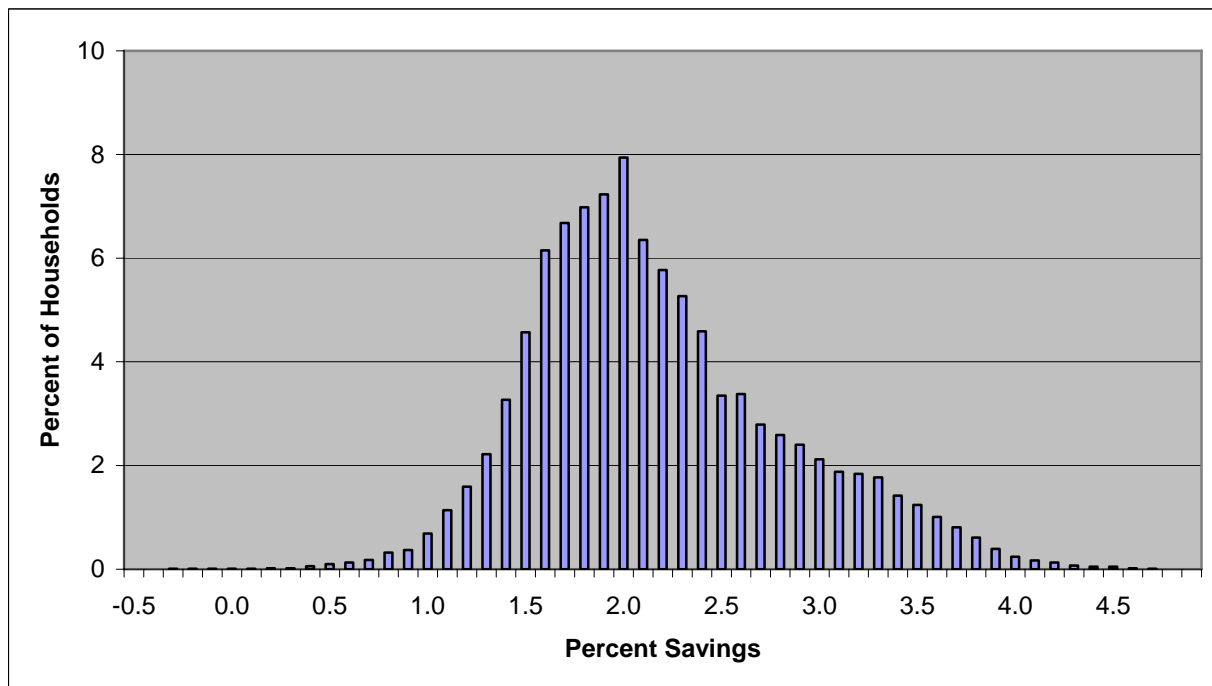
Table 4-8. Parameter estimates using the extended Differenced Linear Fixed Effects (DLFE) Model (Dependent variable: Average daily Kwh; terms affecting treatment response are shaded)

| <i>Variable</i> | <i>Parameter estimate</i> | <i>Standard error</i> | <i>t-statistic</i> |
|--|---------------------------|-----------------------|--------------------|
| <i>Post_t</i> | -2.39049 | 0.35686 | -6.7 |
| <i>Treatment_k·Post_t</i> | -0.72654 | 0.55769 | -1.3 |
| <i>HDDd_t</i> | 0.73135 | 0.00806 | 90.68 |
| <i>HDDd_t·Post_t</i> | -0.14781 | 0.01402 | -10.54 |
| <i>HDDd_t·Treatment_k</i> | 0.00426 | 0.01258 | 0.34 |
| <i>HDDd_t·Treatment_k·Post_t</i> | -0.0348 | 0.02191 | -1.59 |
| <i>CDDd_t</i> | 2.44438 | 0.02179 | 112.18 |
| <i>CDDd_t·Post_t</i> | -0.16331 | 0.03263 | -5.01 |
| <i>CDDd_t·Treatment_k</i> | -0.0234 | 0.03395 | -0.69 |
| <i>CDDd_t·Treatment_k·Post_t</i> | -0.06932 | 0.05077 | -1.37 |
| <i>Pool_k·Post_t</i> | 0.37842 | 0.1758 | 2.15 |
| <i>Pool_k·Treatment_k·Post_t</i> | -0.67809 | 0.27869 | -2.43 |
| <i>Spa_k·Post_t</i> | -0.36664 | 0.35071 | -1.05 |
| <i>Spa_k·Treatment_k·Post_t</i> | -0.06743 | 0.54948 | -0.12 |
| <i>Eheat_k·Post_t</i> | 0.55903 | 0.01316 | 42.46 |
| <i>Eheat_k·Treatment_k·Post_t</i> | 0.00447 | 0.02041 | 0.22 |
| <i>Sqft_k·Post_t</i> | 0.03128 | 0.01438 | 2.18 |
| <i>Sqft_k·Treatment_k·Post_t</i> | 0.02671 | 0.02289 | 1.17 |
| <i>Age_k·Post_t</i> | 0.03545 | 0.00392 | 9.04 |
| <i>Age_k·Treatment_k·Post_t</i> | 0.00223 | 0.0061 | 0.36 |
| <i>Value_k·Post_t</i> | 0.01346 | 0.00555 | 2.42 |
| <i>Value_k·Treatment_k·Post_t</i> | 0.00542 | 0.00887 | 0.61 |
| <i>Envelope_k·Post_t</i> | 0.0192 | 0.13202 | 0.15 |
| <i>Envelope_k·Treatment_k·Post_t</i> | -0.04618 | 0.20694 | -0.22 |
| <i>Template_k·Post_t</i> | 0.03245 | 0.13201 | 0.25 |
| <i>Template_k·Treatment_k·Post_t</i> | -0.04626 | 0.20692 | -0.22 |

4.5 Predicted Distribution of Savings in the Treatment Group

Using the LR model of the previous section, the predicted distribution of savings within the treatment group is presented in Figure 4-4. As noted previously, the average savings is about 2.2%. Predicted percent savings for 50% of all households lie in the interval {1.6, 2.2}, predicted savings for 80% of all households lie in the interval {1.4, 2.9}, and predicted savings for 95% of all households lie in the interval {1.1, 3.5}.

Figure 4-4. Frequency distribution of predicted percent annual energy savings (2007 as base year) within the treatment group



This distribution curve shows that savings are predicted for virtually all individuals, rather than being possible for just a small subset of customers with particular characteristics. It is important to emphasize that this frequency distribution describes *expected* savings within the sample, *conditional* on observed housing characteristics such as square footage of the residence, the presence/absence of a pool, the assessed value of the residence, and so forth, based on the point estimates of the OLS regression of method 2. For a given set of housing characteristics, some households in the real world will generate greater savings and some less than indicated in this modeled distribution.

4.6 Energy Savings of Treatment Households Receiving Monthly Versus Quarterly Reports

A treatment variable not included in the above analysis was the frequency of reports (monthly vs. quarterly) sent to treatment households. This is because the experimental design targeted households with relatively high energy use for monthly reports, and so including this variable would confound the estimated effects of housing characteristics correlated with high energy use.

To examine seasonal impacts by frequency of reporting, we ran the seasonal difference in difference model of Table 4-1 separately for households receiving monthly reports and households receiving quarterly reports. Control households were designated for the different report frequencies based on their level of use to properly match the participant groups. Results are presented in Table 4-9.

Table 4-9. Comparison of Impacts by Season and Frequency of Reports

| <i>Method</i> | <i>Summer Impact</i> | <i>Winter Impact</i> | <i>Shoulder Months Impact</i> | <i>Annual Impact</i> |
|--|----------------------|----------------------|-------------------------------|----------------------|
| <i>Monthly Reports (High Use Customers)</i> | -2.8% | -2.3% | -1.9% | -2.3% |
| <i>Quarterly Reports (Low Use Customers)</i> | -1.4% | -1.6% | -1.4% | -1.6% |
| <i>Overall</i> | -2.6% | -2.2% | -1.7% | -2.2% |

Low use customers receiving quarterly reports show relatively consistent savings throughout the seasons, with slightly higher savings in winter. High use customers receiving monthly reports reflect the overall pattern of savings, showing greatest savings in summer and lowest savings in the shoulder months.

5 AUTHOR BIOGRAPHIES

Daniel Violette, Ph. D. -- Dr. Violette is a Principal with Summit Blue Consulting who has over 20 years of experience in the energy industry. He is a founder and former CEO of Summit Blue and also served as a Vice President and Director with Hagler Bailly Consulting for over 10 years. He has also held officer-level positions with other major companies including serving as a Sr. Vice President with XENERGY, Inc., an energy services company, and with the Management Consulting Services Business Unit of Electronic Data Systems (EDS), one of the largest worldwide management services and technology companies.

Dr. Violette has managed many complex projects resulting in recommendations to senior management regarding actions to be taken related to demand response (DR), pricing and rates, resource planning, and energy efficiency. Current projects include several multi-year efforts examining the role of energy efficiency (EE) and DR in resource planning and development of integrated resource plans that address risk and uncertainty. He also has completed projects for the International Energy Agency on the value of EE and DR in resource planning including hedge/option values and risk management of system costs with a dozen US utilities and 20 countries, and he has authored a report for the Demand Response Research Center (CEC) on an integrated framework for assessing energy efficiency and DR. He is well known for his years of work on demand-side issues including planning, design, evaluation and integration. Dr. Violette has presented testimony and served on expert panels in over 25 regulatory jurisdictions in North America.

Bill Provencher, Ph.D. – Dr. Provencher serves as a full professor in the Department of Agriculture and Applied Economics at the University of Wisconsin-Madison. His published work has two distinct emphases: the dynamic allocation of resources and the valuation of nonmarket goods and services. His current research program focuses on three areas: a) the development of discrete choice models of the consumption of nonmarket goods and services; b) the interaction between socioeconomic and ecological systems; and c) dynamic issues in resource allocation, with attention focused mainly on using statistical methods to recover the dynamic behavior of resource owners. He has served on the board of the Association of Environmental and Resource Economists (AERE), co-edited and served on the editorial council of the *Journal of Environmental Economics and Management* (JEEM), and is currently on the editorial board of *Land Economics*. Dr. Provencher received an undergraduate degree in natural resources at Cornell University, an M.S. degree in forestry at Duke University in 1985, and a Ph.D. in agricultural economics from UC-Davis in 1991.

Mary Klos – Ms. Klos is a Senior Consultant at Summit Blue and has over 20 years of experience in the energy industry. Currently, she leads projects focused on impact analysis of energy efficiency and demand response programs. In her time at the Wisconsin Public Service Corporation, Ms. Klos worked consistently with energy efficiency and demand response issues from a variety of positions, including load forecasting, market research and demand-side management planning. She has worked with generation planners, transmission and distribution planners, rate design experts and marketing professionals to develop an integrated view of the entire DSM effort, and she has testified in rate proceedings and integrated resource planning dockets. Ms. Klos earned a BA in Economics from Beloit College and a Masters in Business Administration from the University of Wisconsin. Ms. Klos is also a certified Statistical Analysis System (SAS) Base Programmer.

APPENDIX A:
DETAILED MODEL RESULTS

Method 2: Linear Regression Base
Model

The REG Procedure
Model: OrigOLS
Dependent Variable: AveDailyKWH

| | |
|------------------------------------|---------|
| Number of Observations Read | 2029885 |
| Number of Observations Used | 2029885 |

| Analysis of Variance | | | | | |
|------------------------|----------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 11 | 46553310 | 4232119 | 14082 | <.0001 |
| Error | 2.03E+06 | 610043717 | 300.53295 | | |
| Corrected Total | 2.03E+06 | 656597027 | | | |

| | | | |
|-----------------------|----------|-----------------|--------|
| Root MSE | 17.33589 | R-Square | 0.0709 |
| Dependent Mean | 31.07693 | Adj R-Sq | 0.0709 |
| Coeff Var | 55.78378 | | |

| Parameter Estimates | | | | | |
|-----------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| Intercept | 1 | 20.03454 | 0.05397 | 371.24 | <.0001 |
| hddD | 1 | 0.73943 | 0.00393 | 188.39 | <.0001 |
| cddD | 1 | 2.49685 | 0.01061 | 235.42 | <.0001 |
| Post | 1 | 1.01504 | 0.08935 | 11.36 | <.0001 |
| PosthddD | 1 | -0.06662 | 0.00664 | -10.04 | <.0001 |
| PostcddD | 1 | -0.30645 | 0.01588 | -19.3 | <.0001 |
| ParticPost | 1 | -0.44838 | 0.13928 | -3.22 | 0.0013 |
| ParticPosthddD | 1 | -0.01815 | 0.01036 | -1.75 | 0.0796 |
| ParticPostcddD | 1 | -0.04983 | 0.0247 | -2.02 | 0.0437 |
| Partic | 1 | -0.34995 | 0.08422 | -4.16 | <.0001 |
| PartichddD | 1 | 0.00277 | 0.00612 | 0.45 | 0.6505 |
| ParticcddD | 1 | -0.03342 | 0.01652 | -2.02 | 0.0431 |

Method 3: Fixed Effects Base
Model

The REG Procedure
Model: base
Dependent Variable: diffaveDailykWh

| | |
|------------------------------------|---------|
| Number of Observations Read | 2029885 |
| Number of Observations Used | 2029885 |

Note: No intercept in model. R-Square is

| Analysis of Variance | | | | | |
|--------------------------|-----------------|------------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 10 | 46287941 | 4628794 | 64523.2 | <.0001 |
| Error | 2.03E+06 | 145619983 | 71.7384 | | |
| Uncorrected Total | 2.03E+06 | 191907924 | | | |

| | | | |
|-----------------------|----------|-----------------|--------|
| Root MSE | 8.46985 | R-Square | 0.2412 |
| Dependent Mean | 1.80E-17 | Adj R-Sq | 0.2412 |
| Coeff Var | 4.71E+19 | | |

| Parameter Estimates | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| diffcddD | 1 | 2.44219 | 0.00518 | 471.24 | <.0001 |
| diffhddD | 1 | 0.73034 | 0.00192 | 380.76 | <.0001 |
| diffPost | 1 | -0.13361 | 0.04369 | -3.06 | 0.0022 |
| diffPosthddD | 1 | -0.01074 | 0.00324 | -3.31 | 0.0009 |
| diffPostcddD | 1 | -0.16486 | 0.00776 | -21.24 | <.0001 |
| diffParticPost | 1 | -0.32591 | 0.0681 | -4.79 | <.0001 |
| diffParticPosthddD | 1 | -0.02453 | 0.00506 | -4.85 | <.0001 |
| diffParticPostcddD | 1 | -0.06754 | 0.01208 | -5.59 | <.0001 |
| diffParticHDDd | 1 | 0.0041 | 0.00299 | 1.37 | 0.1704 |
| diffParticCDDd | 1 | -0.02305 | 0.00807 | -2.86 | 0.0043 |

Method 2: Linear Regression
Expanded Model

The REG Procedure
Model: HeterOLS
Dependent Variable: AveDailyKWH

| | |
|---|---------|
| Number of Observations Read | 2029885 |
| Number of Observations Used | 2025212 |
| Number of Observations with Missing Values | 4673 |

| Analysis of Variance | | | | | |
|----------------------|----------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 41 | 245023876 | 5976192 | 29501.5 | <.0001 |
| Error | 2.03E+06 | 410244298 | 202.57277 | | |
| Corrected Total | 2.03E+06 | 655268174 | | | |

| | | | |
|-----------------------|----------|-----------------|--------|
| Root MSE | 14.23281 | R-Square | 0.3739 |
| Dependent Mean | 31.09019 | Adj R-Sq | 0.3739 |
| Coeff Var | 45.7791 | | |

| Parameter Estimates | | | | | |
|----------------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| Intercept | 1 | 2.58923 | 0.08741 | 29.62 | <.0001 |
| Post | 1 | 1.4126 | 0.14112 | 10.01 | <.0001 |
| ParticPost | 1 | -0.1095 | 0.22251 | -0.49 | 0.6226 |
| Partic | 1 | 1.16059 | 0.13963 | 8.31 | <.0001 |
| cddD | 1 | 2.47496 | 0.00872 | 283.91 | <.0001 |
| PostcddD | 1 | -0.25433 | 0.01305 | -19.49 | <.0001 |
| ParticPostcddD | 1 | -0.06357 | 0.02031 | -3.13 | 0.0017 |
| ParticcddD | 1 | -0.02555 | 0.01358 | -1.88 | 0.0599 |
| hddD | 1 | 0.42534 | 0.00334 | 127.39 | <.0001 |
| PosthddD | 1 | -0.03041 | 0.00564 | -5.39 | <.0001 |
| ParticPosthddD | 1 | -0.01879 | 0.00882 | -2.13 | 0.0331 |
| PartichddD | 1 | -0.00836 | 0.00522 | -1.6 | 0.109 |
| pool | 1 | 10.90364 | 0.04539 | 240.25 | <.0001 |
| PostPool | 1 | 0.01959 | 0.07028 | 0.28 | 0.7805 |
| ParticPostPool | 1 | -0.69719 | 0.1114 | -6.26 | <.0001 |
| ParticPool | 1 | -0.12378 | 0.07189 | -1.72 | 0.0851 |
| spa | 1 | 0.7963 | 0.09075 | 8.78 | <.0001 |
| PostSpa | 1 | 0.03275 | 0.14022 | 0.23 | 0.8153 |
| ParticPostSpa | 1 | -0.31411 | 0.21966 | -1.43 | 0.1527 |
| ParticSpa | 1 | 0.40093 | 0.14198 | 2.82 | 0.0047 |
| ElecHeatHDDd | 1 | 1.26684 | 0.00345 | 367.46 | <.0001 |
| PostElecHeatHDDd | 1 | -0.06718 | 0.00586 | -11.46 | <.0001 |
| ParticPostElecHeatHDDd | 1 | -0.01397 | 0.00909 | -1.54 | 0.1243 |
| ParticElecHeatHDDd | 1 | -0.02382 | 0.00534 | -4.46 | <.0001 |
| sqft_00 | 1 | 0.7717 | 0.00371 | 208.24 | <.0001 |
| PostSqft_00 | 1 | -0.02808 | 0.00575 | -4.88 | <.0001 |
| ParticPostSqft_00 | 1 | -0.01467 | 0.00916 | -1.6 | 0.1094 |
| ParticSqft_00 | 1 | -0.03334 | 0.0059 | -5.65 | <.0001 |
| age | 1 | -0.00408 | 0.00102 | -4.02 | <.0001 |
| Postage | 1 | -0.0167 | 0.00158 | -10.57 | <.0001 |
| ParticPostAge | 1 | 0.00116 | 0.00246 | 0.47 | 0.6359 |
| Particage | 1 | -0.01144 | 0.00158 | -7.24 | <.0001 |
| house_value_0000 | 1 | 0.07725 | 0.00143 | 54.04 | <.0001 |
| Posthouse_value_0000 | 1 | 0.0142 | 0.00222 | 6.4 | <.0001 |
| ParticPostHouse_value_0000 | 1 | 0.00636 | 0.00354 | 1.8 | 0.0724 |
| Partichouse_value_0000 | 1 | -0.00981 | 0.00228 | -4.31 | <.0001 |
| PostTemplate | 1 | -0.06236 | 0.04043 | -1.54 | 0.123 |
| ParticPostTemplate | 1 | 0.07479 | 0.07543 | 0.99 | 0.3214 |
| ParticTemplate | 1 | -0.18351 | 0.04088 | -4.49 | <.0001 |
| PostEnvelope | 1 | 0.06717 | 0.04043 | 1.66 | 0.0967 |
| ParticPostEnvelope | 1 | -0.1137 | 0.07544 | -1.51 | 0.1318 |
| ParticEnvelope | 1 | 0.02942 | 0.04088 | 0.72 | 0.4718 |

Method 3: Fixed Effects Expanded Model

The REG Procedure
 Model: HeterDF
 Dependent Variable: AveDailyKWH

| | |
|--|---------|
| Number of Observations Read | 2029885 |
| Number of Observations Used | 2025212 |
| Number of Observations with Missing Values | 4673 |

Note: No intercept in model. R-Square is redefined.

| Analysis of Variance | | | | | |
|----------------------|----------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 26 | 50192832 | 1930494 | 1525.61 | <.0001 |
| Error | 2.03E+06 | 2562644528 | 1265.38724 | | |
| Uncorrected Total | 2.03E+06 | 2612837360 | | | |

| | | | |
|----------------|-----------|----------|--------|
| Root MSE | 35.57228 | R-Square | 0.0192 |
| Dependent Mean | 31.09019 | Adj R-Sq | 0.0192 |
| Coeff Var | 114.41643 | | |

| Parameter Estimates | | | | | |
|--------------------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| diffPost | 1 | -2.39049 | 0.35686 | -6.7 | <.0001 |
| diffParticPost | 1 | -0.72654 | 0.55769 | -1.3 | 0.1927 |
| diffcddD | 1 | 2.44438 | 0.02179 | 112.18 | <.0001 |
| diffPostcddD | 1 | -0.16331 | 0.03263 | -5.01 | <.0001 |
| diffParticPostcddD | 1 | -0.06932 | 0.05077 | -1.37 | 0.1721 |
| diffParticCDDd | 1 | -0.0234 | 0.03395 | -0.69 | 0.4906 |
| diffhddD | 1 | 0.73135 | 0.00806 | 90.68 | <.0001 |
| diffPosthddD | 1 | -0.14781 | 0.01402 | -10.54 | <.0001 |
| diffParticPosthddD | 1 | -0.0348 | 0.02191 | -1.59 | 0.1122 |
| diffParticHDDd | 1 | 0.00426 | 0.01258 | 0.34 | 0.7349 |
| diffPostPool | 1 | 0.37842 | 0.1758 | 2.15 | 0.0314 |
| diffParticPostPool | 1 | -0.67809 | 0.27869 | -2.43 | 0.015 |
| diffPostSpa | 1 | -0.36664 | 0.35071 | -1.05 | 0.2958 |
| diffParticPostSpa | 1 | -0.06743 | 0.54948 | -0.12 | 0.9023 |
| diffPostElecHeatHDDd | 1 | 0.55903 | 0.01316 | 42.46 | <.0001 |
| diffParticPostElecHeatHDDd | 1 | 0.00447 | 0.02041 | 0.22 | 0.8267 |
| diffPostSqft_00 | 1 | 0.03128 | 0.01438 | 2.18 | 0.0296 |
| diffParticPostSqft_00 | 1 | 0.02671 | 0.02289 | 1.17 | 0.2434 |
| diffPostAge | 1 | 0.03545 | 0.00392 | 9.04 | <.0001 |
| diffParticPostAge | 1 | 0.00223 | 0.0061 | 0.36 | 0.7151 |
| diffPostHouse_Value_0000 | 1 | 0.01346 | 0.00555 | 2.42 | 0.0154 |
| diffParticPostHouse_Value_0000 | 1 | 0.00542 | 0.00887 | 0.61 | 0.5411 |
| diffPostTemplate | 1 | 0.03245 | 0.13201 | 0.25 | 0.8058 |
| diffParticPostTemplate | 1 | -0.04626 | 0.20692 | -0.22 | 0.8231 |
| diffPostEnvelope | 1 | 0.0192 | 0.13202 | 0.15 | 0.8844 |
| diffParticPostEnvelope | 1 | -0.04618 | 0.20694 | -0.22 | 0.8234 |

Base Model for Quarterly Report
Group

The REG Procedure
Model: Qtrly
Dependent Variable: diffaveDailykWh

| | |
|-----------------------------|--------|
| Number of Observations Read | 240168 |
| Number of Observations Used | 240168 |

Note: No intercept in model. R-Square is redefined.

| Analysis of Variance | | | | | |
|----------------------|--------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 5 | 1901600 | 380320 | 19722.3 | <.0001 |
| Error | 240163 | 4631247 | 19.28376 | | |
| Uncorrected Total | 240168 | 6532846 | | | |

| | | | |
|----------------|-----------|----------|--------|
| Root MSE | 4.39133 | R-Square | 0.2911 |
| Dependent Mean | -4.51E-18 | Adj R-Sq | 0.2911 |
| Coeff Var | -9.73E+19 | | |

| Parameter Estimates | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| diffPost | 1 | 0.30321 | 0.05111 | 5.93 | <.0001 |
| diffcddD | 1 | 1.39007 | 0.00593 | 234.31 | <.0001 |
| diffPostcddD | 1 | -0.09566 | 0.00897 | -10.66 | <.0001 |
| diffhddD | 1 | 0.34707 | 0.0022 | 157.56 | <.0001 |
| diffPosthddD | 1 | -0.00083494 | 0.00378 | -0.22 | 0.8253 |

| Covariance of Estimates | | | | | |
|-------------------------|--------------|--------------|--------------|-------------|--------------|
| Variable | diffPost | diffcddD | diffPostcddD | diffhddD | diffPosthddD |
| diffPost | 0.002612615 | 0.000141865 | -0.000385561 | 5.94168E-05 | -0.000172727 |
| diffcddD | 0.000141865 | 3.51952E-05 | -0.000035206 | 9.21E-06 | -9.21E-06 |
| diffPostcddD | -0.000385561 | -0.000035206 | 8.04653E-05 | -9.21E-06 | 2.53404E-05 |
| diffhddD | 5.94168E-05 | 9.21E-06 | -9.21E-06 | 4.85E-06 | -4.86E-06 |
| diffPosthddD | -0.000172727 | -9.21E-06 | 2.53404E-05 | -4.86E-06 | 1.43038E-05 |

Base Model for Monthly Report
Group

The REG Procedure
Model: Month
Dependent Variable: diffaveDailykWh

| | |
|-----------------------------|--------|
| Number of Observations Read | 586698 |
| Number of Observations Used | 586698 |

Note: No intercept in model. R-Square is redefined.

| Analysis of Variance | | | | | |
|----------------------|--------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 5 | 18214496 | 3642899 | 40555.2 | <.0001 |
| Error | 586693 | 52700128 | 89.82573 | | |
| Uncorrected Total | 586698 | 70914624 | | | |

| | | | |
|----------------|----------|----------|--------|
| Root MSE | 9.47764 | R-Square | 0.2569 |
| Dependent Mean | 3.17E-17 | Adj R-Sq | 0.2568 |
| Coeff Var | 2.99E+19 | | |

| Parameter Estimates | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| diffPost | 1 | -0.56019 | 0.06894 | -8.13 | <.0001 |
| diffcddD | 1 | 2.84333 | 0.00824 | 345.22 | <.0001 |
| diffPostcddD | 1 | -0.31349 | 0.01225 | -25.59 | <.0001 |
| diffhddD | 1 | 0.89418 | 0.00305 | 292.81 | <.0001 |
| diffPosthddD | 1 | -0.0613 | 0.00514 | -11.93 | <.0001 |

| Covariance of Estimates | | | | | |
|-------------------------|--------------|--------------|--------------|--------------|--------------|
| Variable | diffPost | diffcddD | diffPostcddD | diffhddD | diffPosthddD |
| diffPost | 0.004752634 | 0.000276504 | -0.000708873 | 0.000114856 | -0.000314899 |
| diffcddD | 0.000276504 | 6.78382E-05 | -0.000067851 | 1.77594E-05 | -0.000017764 |
| diffPostcddD | -0.000708873 | -0.000067851 | 0.000150131 | -0.000017762 | 4.66113E-05 |
| diffhddD | 0.000114856 | 1.77594E-05 | -0.000017762 | 9.33E-06 | -9.33E-06 |
| diffPosthddD | -0.000314899 | -0.000017764 | 4.66113E-05 | -9.33E-06 | 2.63913E-05 |